

# Slanted edge vs. Siemens star MTF calculations

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The goal of this document is to compare the effects of demosaicing and sharpening (or bilateral filtering) on MTF measurements for the two most widely used test patterns — the slanted edge and the sinusoidal Siemens star. We are particularly interested in investigating the belief that the Siemens star (or sinusoidal patterns in general) is relatively unaffected by sharpening, so that it approximates the original unsharpened system response.

## Definitions

**Sharpening** — A process for making an image appear sharper by taking the original signal, then subtracting shifted, reduced-amplitude replicas (standard sharpening), or subtracting a reduced-amplitude, gaussian blurred version (unsharp masking or USM). These methods are uniform and (usually) [linear](#). Described in detail in the [Sharpening page](#).

**Bilateral filtering** — a type of filtering where regions of the image close to fine details or edges are sharpened (high frequencies are boosted), but regions away from edges are lowpass-filtered (high frequencies are attenuated). The purpose is to reduce visible noise while maintaining a sharp appearance. Nonuniform as well as nonlinear. Almost universal in JPEG files from consumer cameras. Can usually be detected by the presence of a strong peak in a plot the spatially dependent noise amplitude,  $\sqrt{N(x)}$ . This plot is a part of the [Image information metrics](#).

**Demosaicing** — the process of transforming the signal from an image sensor (“mosaiced” with a color filter array, typically a (RGRG; GBGB...) Bayer array, into a three-channel RGB image. A key function of [raw conversion](#), which also includes white balance, color correction, gamma-encoding, and often sharpening and noise reduction. Demosaicing is a type of interpolation that, in its simplest form, lowpass filters the signal (removes high frequency energy). Sophisticated demosaicing algorithms use detected edges to try to recover this energy. Demosaicing quality is often better when performed by a raw conversion program, rather than in the camera.

**Nyquist frequency** —  $f_{Nyq} = 0.5$  Cycles/Pixel, the highest frequency where the original signal can be reconstructed. Information above Nyquist is of interest because it indicates that [aliasing](#) artifacts might be present.

To explore the differences in performance between slanted edges and Siemens stars, we compare results from several images (simulated and from different cameras with different types of demosaicing). We found that sharpening behavior and response near and beyond the Nyquist frequency ( $f_{Nyq} = 0.5$  C/P) are separate issues.



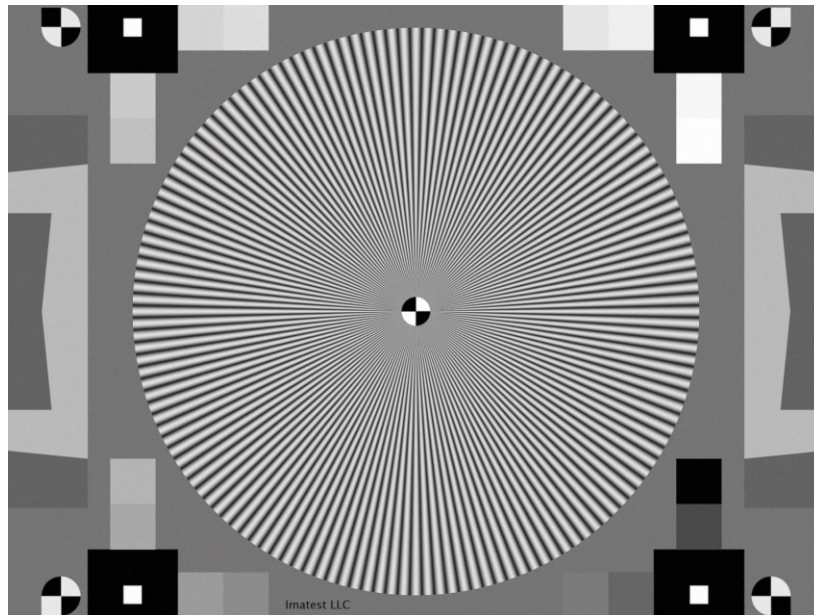
## Image comparisons

### 1. Simulated image: no demosaicing

We applied a few tricks to obtain a fair comparison between the two patterns.

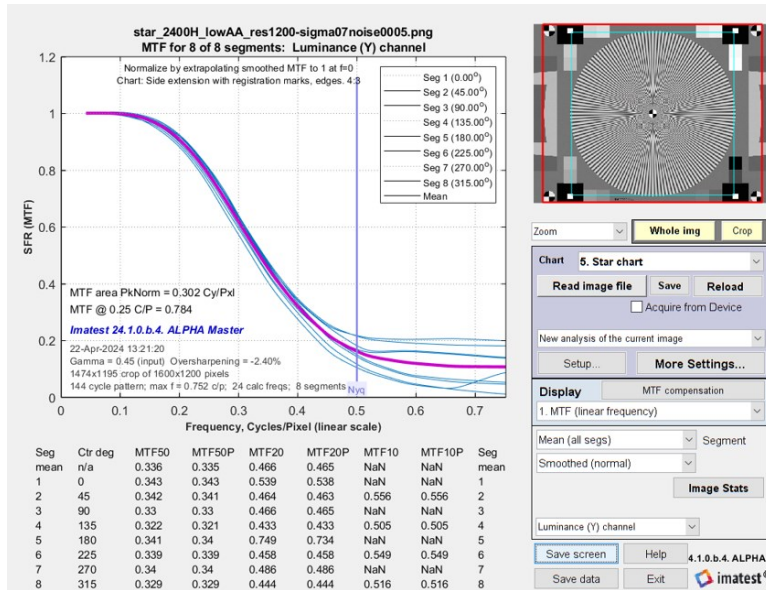
A 2400-pixel high image of a 50:1 contrast sinusoidal Siemens star (the ISO standard), which also contained 4:1 contrast slanted edges, was created with Imatest [Test Charts](#). We adjusted the amount of anti-aliasing on the star to give results consistent with the edges.

To make the comparison fairer, we resized the 2400-pixel high images to 1200 pixels high using [Irfanview](#), with the sharpen box checked. This should remove differences due to the anti-aliasing routines for the star and edges, which are close but not identical. For comparison with real images, we added a small amount of gaussian blur (sigma = 0.7 pixels) and a tiny amount of gaussian noise (sigma = 0.0005 pixels).

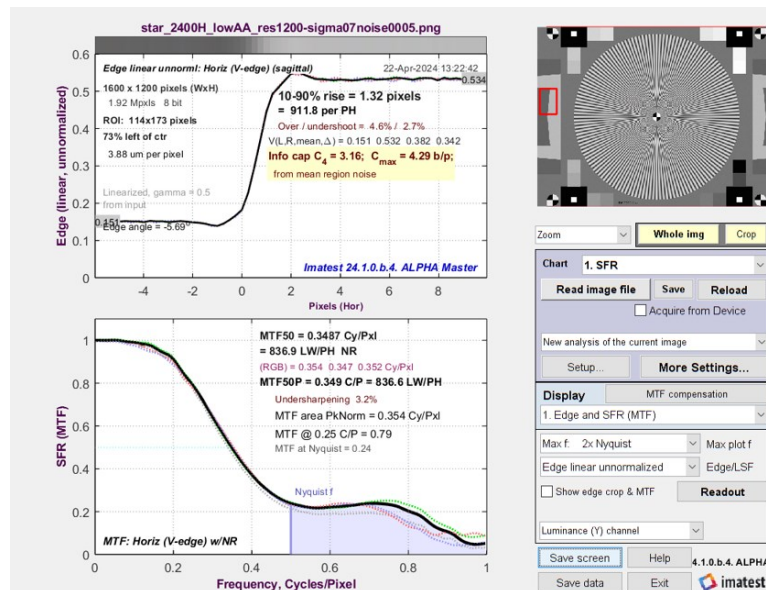


**Simulated image with Siemens star and slanted edge, resized from 2400 to 1200 pixels high,  
Blur sigma = 0.7 pixels; noise sigma 0.0005.**

# 1. Simulated image: no demosaicing (continued)



Results for simulated Siemens star. Mean MTF50 = 0.336.



Results for simulated slanted edge (same image as star, above). MTF50 = 0.349.  
(Note the modest sharpening from the Irfanview resizing.)

Both patterns have significant (but not identical) response above  $f_{Nyq}$ . It is possible that some of the response is an artifact of the resizing, but the important thing is that resizing makes the sine and edge response more consistent.

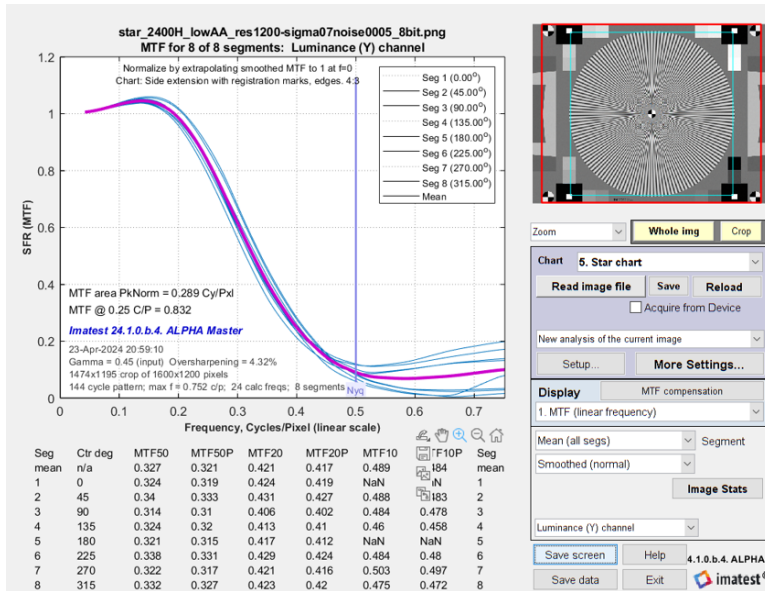
The results are close, but the average result for the star has slightly lower MTF. (MTF50 = 0.336 for the star vs. 0.349 for the edge; around 0.17 at  $f_{Nyq}$  for the star vs. 0.23 for the edge). Note that the highest MTFs for the star (for specific angular regions) were very close to the edge.

All slanted-edge plots have a maximum display frequency of  $1 C/P$  ( $2 \times f_{Nyq}$ ), but the maximum for the star plot depends on the image size.

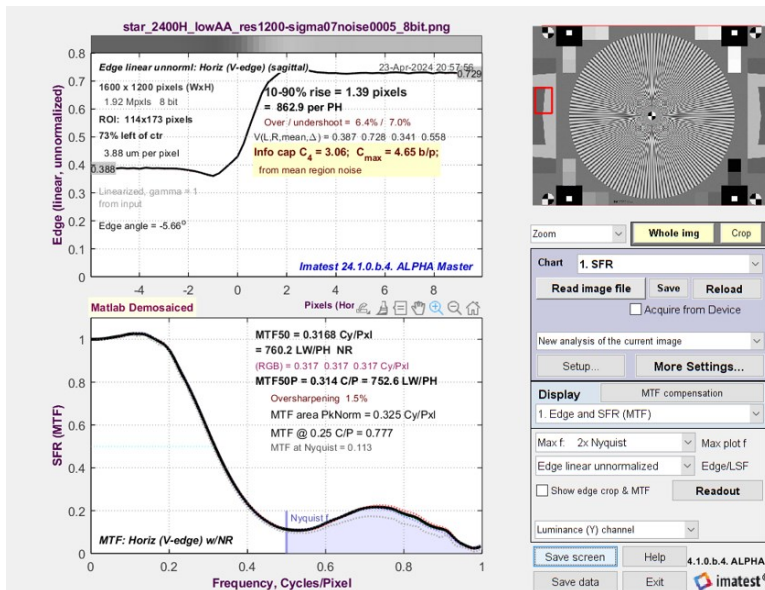
## 2. Simulated image: converted to 8-bit (monochrome) and demosaiced

The following two results are for the image in 1 (above), converted to monochrome (from 24 to 8 bit depth), then demosaiced using the [MATLAB demosaicing routine](#).

(Note that the 8-bit undemosaiced images had MTF50 = 0.336 for the star (identical) and MTF50 = 0.3505 for the slanted edge (extremely close).)



### Results for simulated & demosaiced Siemens star

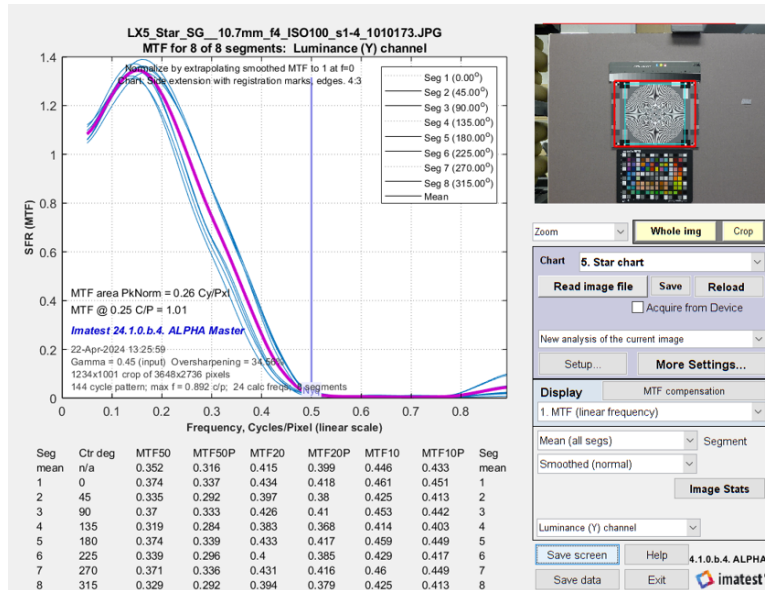


### Results for simulated & demosaiced slanted edge (same image as star, above)

There were relatively small changes in the response. The star had lower response above  $f_{Nyq}$  than the edge.

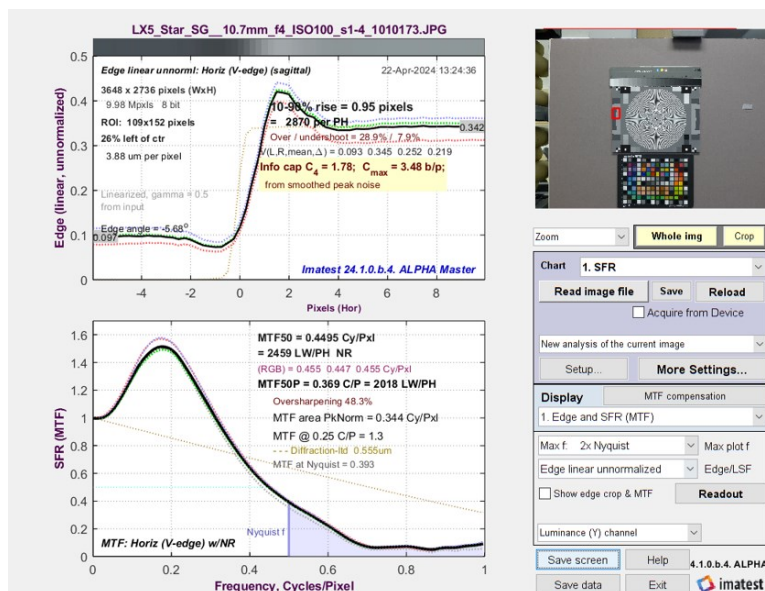


### 3. JPEG image from compact digital camera

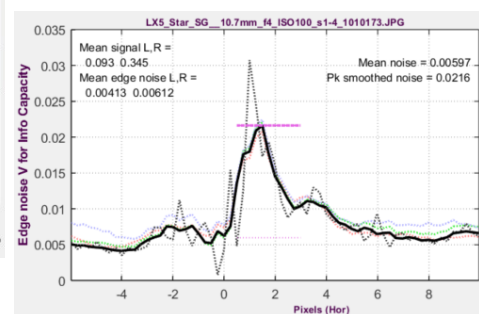


Demosaicing and other raw-conversion functions were performed in the camera. (The demosaicing algorithm is different from image 2, above.)

Results for Siemens star from JPEG.  
No response above Nyquist.



The plot below shows the spatially dependent noise amplitude,  $\sqrt{N(x)}$ . As we discuss in the documentation for [Image information metrics](#), a strong peak indicates the presence of bilateral filtering.



Results for slanted edge from the same JPEG.

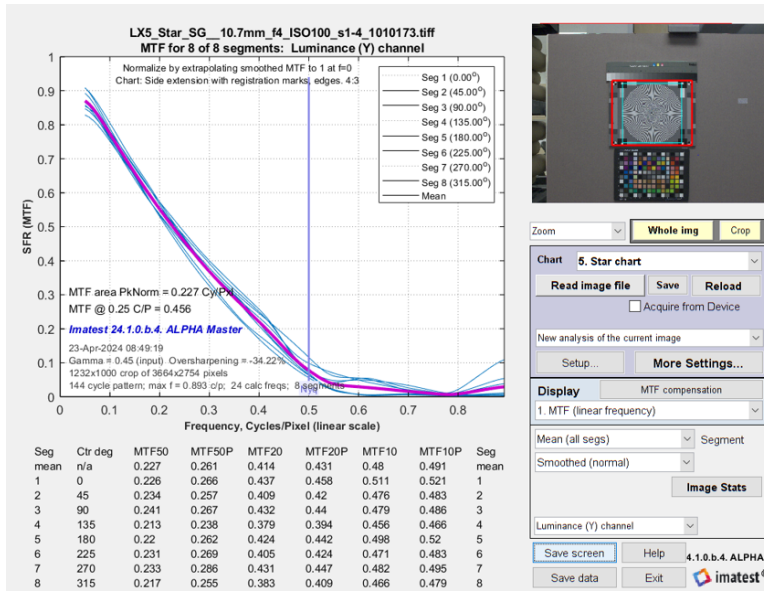
Right: noise amplitude,  $\sqrt{N(x)}$ .

The Siemens star and slanted edge appear to be sharpened by similar amounts (just a slightly larger MTF peak for the edge) with radius  $\approx 2$  in both cases, even though the noise amplitude plot on the right clearly indicates bilateral filtering—which could reduce sharpening for the Siemens star.

The big difference in the two results is that **the star has nearly zero response above Nyquist ( $f_{Nyq} = 0.5$  C/P)**, while the edge has very significant response above Nyquist (0.4 at  $f_{Nyq}$ ). The low response for the star and the high response for the edge could be due either to

- (a) interpolation in the camera's fast but low-quality demosaicing (most likely), or
- (b) bilateral filtering, which is definitely present.

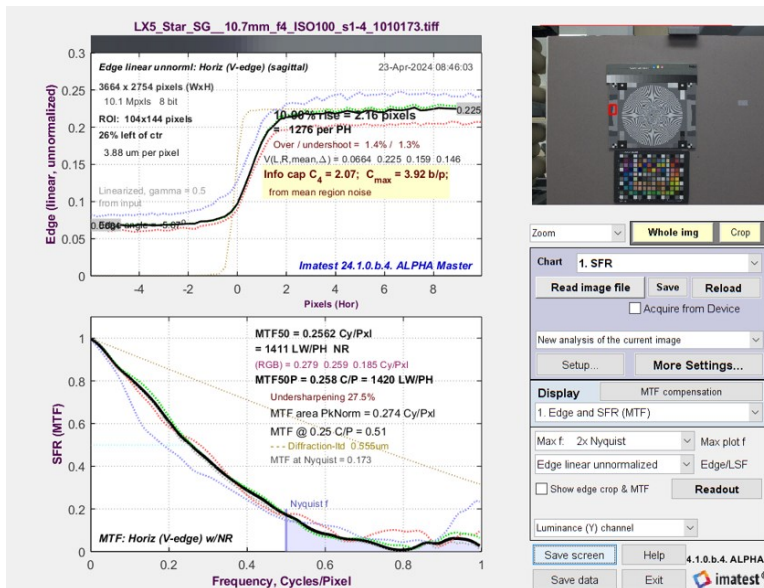
## 4. LibRaw-converted (unsharpened) image from compact digital camera



The same image as the JPEG in 3 was converted with LibRaw. This is the unsharpened result.

Information capacity = 3.4 bits/pixel.

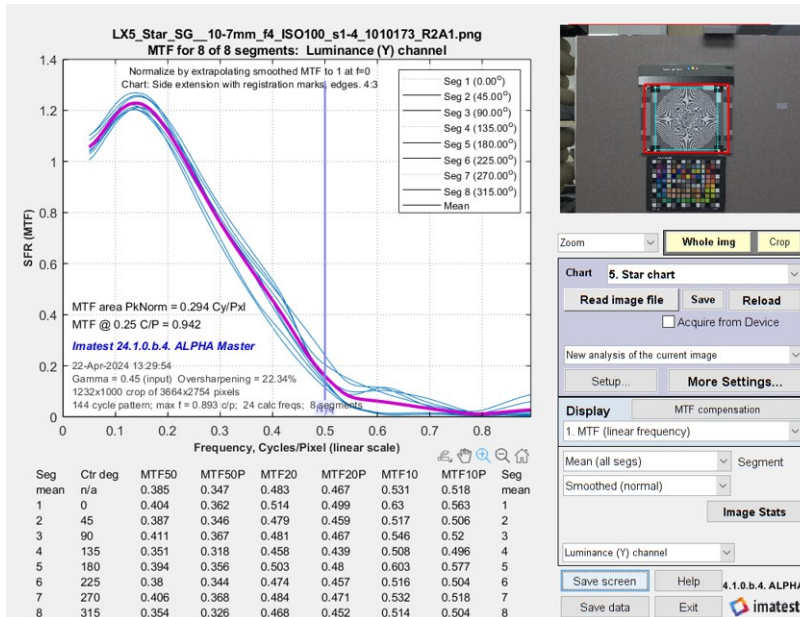
### Results for Siemens star from the LibRaw-converted image (unsharpened)



### Results for slanted edge from the LibRaw-converted image (unsharpened)

Results are similar, but MTF50 for the edge (0.256 C/P) is somewhat larger than for the star (0.227) MTF at Nyquist is approximately 0.18 for the edge vs. 0.07 for the star. Unlike the camera JPEG, there is some response above Nyquist for the star, but it is lower than for the edge.

## 5. LibRaw-converted & sharpened image from compact digital camera

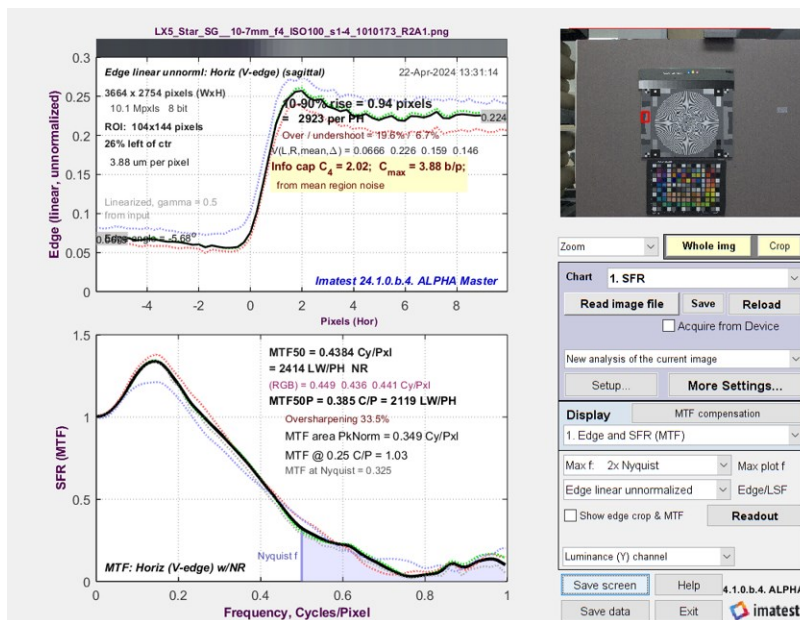


The same image as the JPEG in 3 was saved as raw and converted with LibRaw. A modest amount of sharpening (R2A1; Radius = 2, Amount = 1) was applied to make it easier to compare with the JPEG results. (Saturation was an issue with more sharpening.)

Information capacity = 3.36 bits/pixel. Unchanged from the unsharpened image.

Results for Siemens star from the

sharpened LibRaw-converted image



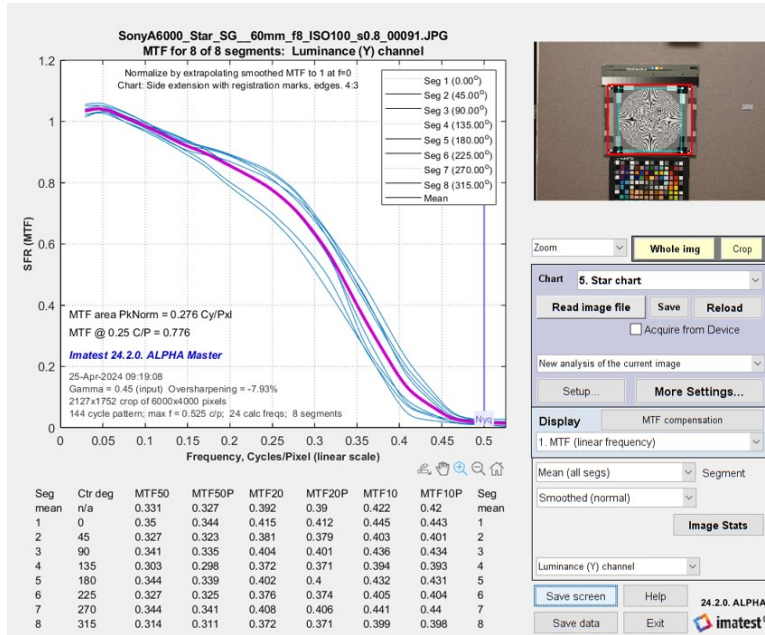
Results for slanted edge from the sharpened LibRaw-converted image.

The key thing to note is that sharpening affects *both* star and edge MTF, but the edge is slightly more strongly sharpened. Unlike the JPEG, the star has some response above Nyquist. Information capacity for both patterns is unaffected by sharpening. (It is slightly lower for the star than  $C_{max}$  for the edge.)

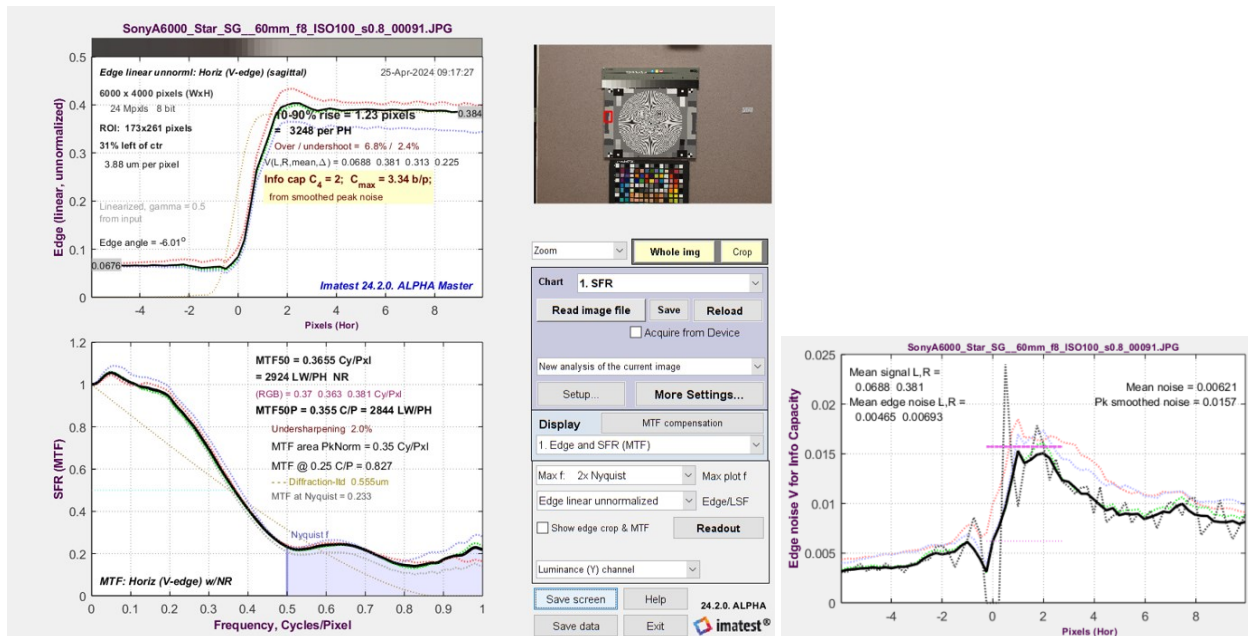


## 6. JPEG image from 24-megapixel Micro Four-Thirds digital camera

Because this camera is from a different manufacturer from 3, we expect the in-camera demosaicing routine to behave differently.



Results for Siemens star from JPEG. As with 3, there is no response above Nyquist.



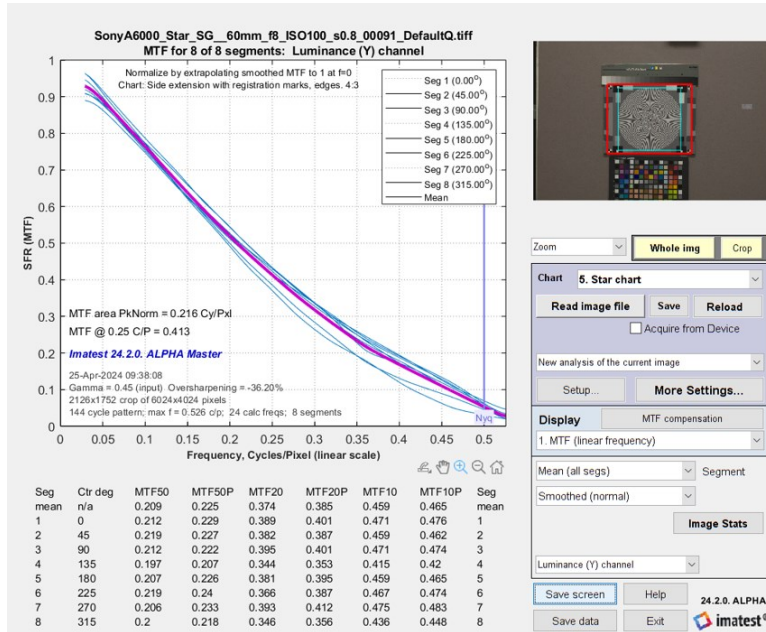
Results for slanted edge from the same JPEG. Right: noise amplitude ( $\sqrt{N(x)}$ ).

The artifacts above  $f_{Nyq}$  (0.5 C/P) are particularly severe.

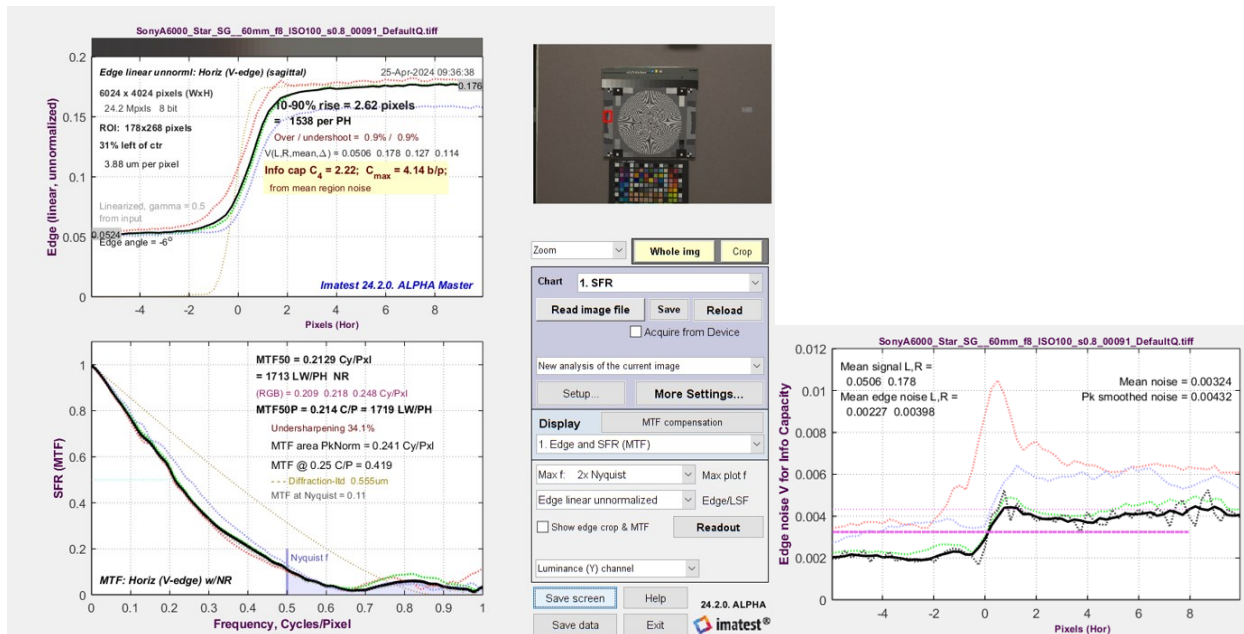
Both response curves show a bump from moderate amounts of sharpening. Bilateral filtering, which is common in JPEGs from cameras, does not appear to be strong.

## 7. LibRaw-converted (unsharpened) image from 24-megapixel digital camera

The same image as the JPEG was converted with LibRaw. This is the unsharpened result.



### Results for Siemens star from the LibRaw-converted image (unsharpened)



Left: Results for slanted edge from the LibRaw-converted image (unsharpened)

Right: Noise amplitude ( $\sqrt{N(x)}$ ) has no peak (indicating no bilateral filtering).

Results are similar, but the MTF50 for the edge (0.213 C/P) is nearly identical to for the star (0.209). However, MTF at  $f_{Nyq}$  is double for the edge (0.11 vs. 0.05), but the absolute difference is low.

## Verification of the slanted-edge calculation

There are two places on the Imatest website where the slanted-edge calculation is verified.

<https://www.imatest.com/2015/04/lsf-correction-factor-for-slanted-edge-mtf-measurements/#verification>. This is for an idealized edge that changes from light to dark linearly over a distance of one pixel. Here is the result for the slanted-edges in the latest Siemens star (with edge) Test Charts pattern.

The equations for the MTF are on the [above link](#). The expected value is  $MTF(f_{Nyq}) = 0.6366$ , which is very close to the result shown on the right (0.642).

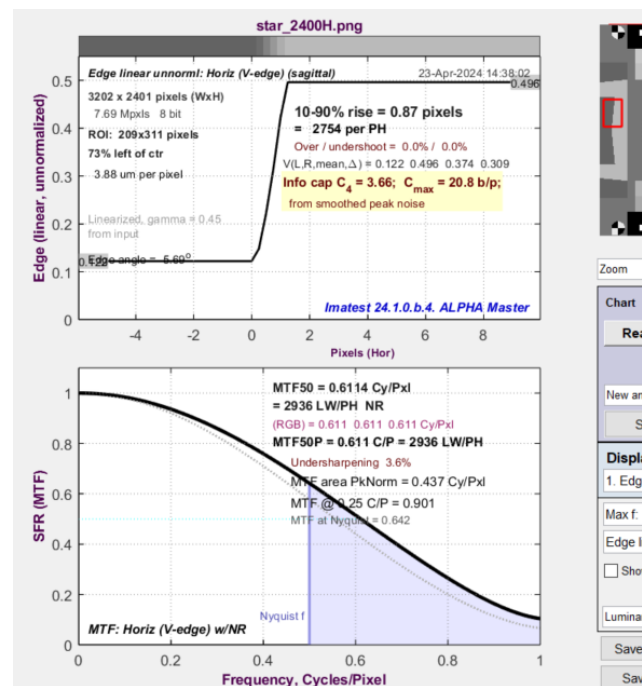
The second link, which compares a somewhat blurred sine pattern and edge, is

[https://www.imatest.com/docs/validating\\_slanted\\_edge/](https://www.imatest.com/docs/validating_slanted_edge/). Slanted-edges are compared with sine patterns, but the edge rise distance on this page is not exactly one pixel, so results are somewhat different from the previous link.

## Summary

In preparing this document we realized that two separate issues affect the comparison of slanted edges with Siemens stars.

- 1. Sensitivity to sharpening** — Depending on how you classify them, there are two or three types of sharpening.
  - a. Uniform sharpening, which can either be standard or USM (unsharp mask),
  - b. Bilateral filtering (described in documentation for [Image information metrics](#)), where areas near sharp edges are sharpened, but smooth areas (away from edges) may be smoothed (lowpass-filtered or blurred). Bilateral filters are nearly universal in JPEG images from consumer cameras. The amount of lowpass filtering, sharpening, and the transition threshold varies for different cameras.
- 2. Response at and above Nyquist** ( $f_{Nyq} = 0.5 \text{ C/P}$ ) — affected by the demosaicing algorithm, which can be different when performed in the camera or in a separate program on a computer (not in the camera; Imatest uses LibRaw).
  - a. In-camera demosaicing (used to produce JPEGs) are optimized for maximum speed and minimum power consumption. Quality may be compromised.
  - b. Demosaicing programs run on computers are primarily optimized for quality; speed is less critical.



## Image summary

#	Source	Processing
1	Simulated (Test Charts)	Resize 2400H → 1200H, blur $\sigma = 0.7$ , noise $\sigma = 0.0005$
2	#1	Convert to 8-bit monochrome, <a href="#">MATLAB demosaicing</a>
3	Compact camera (Lumix LX5)	JPEG (sharpened)
4	Compact camera (Lumix LX5)	Raw, LibRaw demosaicing
5	Compact camera (Lumix LX5)	Raw, LibRaw, USM sharpened R2A1 to compare with #3
6	Micro 4/3 camera (Sony A6000)	JPEG (sharpened)
7	Micro 4/3 camera (Sony A6000)	Raw, LibRaw demosaicing

## Results — Sensitivity to sharpening

Images 3, 5, and 6 are sharpened. 3 and 6 are sharpened in two different cameras. 5 was demosaiced with LibRaw and uniformly sharpened (uniformly) using Unsharp Mask with R2A1; Radius = 2, Amount = 1.

The in-camera JPEG from compact digital cameras 3 and 6 show similar sharpening for the edge and star (slightly more for the edge). Because JPEGs from most cameras have bilateral filtering (nonuniform sharpening) we expected to see a larger difference. The dramatic difference at  $f_{Nyq}$ , where there is strong response for the edge, but essentially zero response for the star, is a separate issue, described below.

**The Siemens star is only slightly less sensitive to sharpening than the slanted edge.**

## Results — Response at and above Nyquist ( $f_{Nyq} = 0.5 C/P$ )

Response near and above Nyquist is strongly affected by demosaicing, which can vary significantly between cameras and external raw converters.

**Demosaicing** — in its simplest form is an interpolation process, which acts as a lowpass filter. High quality demosaicing is aware of detail in the individual channels (especially edges) and adjusts the interpolation to maintain detail, especially for edges.

**Results** — The response of the simulated, undemosaiced image 1 is relatively close for the star and edge, with the edge having slightly larger response at  $f_{Nyq}$  (0.23 vs. 0.17). This is our baseline (results with no image processing).

When image 1 is interpreted as Bayer raw and demosaiced using the high-quality [MATLAB demosaicing routine](#) (image 2), the changes are relatively small. MTF at  $f_{Nyq}$  is slightly lower for both cases, but the comparison is unchanged.

Images 4, 5, and 7, stored in raw format then demosaiced by LibRaw (high quality), have responses comparable to images 1 and 2, but the MTF at Nyquist is higher for the edge relative to the star — around double.

Images 3 and 6, JPEGs converted in the cameras, have *BIG* differences between edges and stars. There is essentially no response above Nyquist for the stars. But for edges, MTF above Nyquist is much larger than for LibRaw-converted images. This response appears to be artifacts resulting from low-quality in-camera demosaicing.

Images 3 and 6 are examples of low quality demosaicing — common in camera JPEGs. Edge MTF is aggressively maintained, but artifacts are created in the process. MTF for the stars is strongly attenuated for  $f \geq f_{Nyq}$ . [Note: this is unrelated to JPEG compression.] By comparison, LibRaw-converted images 4, 5, and 7 maintain edge response with smaller artifacts and maintain some star response above Nyquist (absent in the camera JPEGs).

**For in-camera raw conversion (which may have relatively low quality),  
MTF for  $f \geq f_{Nyq}$  is often boosted (with artifacts) for slanted edges,  
but severely attenuated (effectively removed) for Siemens stars.**

**Neither shows the whole picture.**

## So which pattern is better?

Tricky question. Both are good, and they produce different results because demosaicing algorithms respond differently to the different patterns.

**But as founder of *Imatest* and author of this document, I offer an opinion. *I prefer slanted edge measurements for several reasons.***

- Our perception of sharpness is largely based on edges, not on sinusoidal patterns.
- Demosaicing routines (especially off-camera) recover more of the sharpness lost to interpolation for edges than for sinusoidal features (such as the Siemens star). Separate raw converter programs do this better. In-camera demosaicing is usually inferior, often creating artifacts in slanted edges at  $f \geq f_{Nyq}$  while severely attenuating high frequency response for sinusoidal patterns. With in-camera demosaicing, neither pattern produces results for  $f$  near or  $\geq f_{Nyq}$  sufficient to characterize the camera. Both results paint a fuller picture.
- Slanted-edge analysis has several other well-known advantages. Edges are generally smaller, making it practical to map sharpness over the surface of the image. Computations are faster. And for 4:1 contrast edges (specified by ISO 12233), saturation is rarely a problem, except when sharpening is excessive. And when sharpening is excessive, large spikes (“halos”) near edges represent the actual performance of the camera quite well.
- Low resolution images (common in medical endoscopes) may have insufficient resolution with Siemens stars to allow space for a low frequency reference, which is critical for calculating MTF. Light falloff (vignetting) can also adversely affect the low frequency reference. With slanted edges, a low frequency reference is taken for granted because it is easy to obtain.
- **Image information metrics** (measurements related to information capacity, including object and edge detection performance) are calculated using MTF for  $f < f_{Nyq}$  (frequencies where the two



patterns yield similar results). These metrics are currently available for slanted edges. They could be added to Siemens star results at customer request, but it would require some effort.

- The star response represents a wider range of angles than edges, but we have rarely observed new information of interest over a range of angles. All the star plots above contain results for 8 angular regions, and results for the regions are very close. Of course, it is possible that something surprising might show up in the star that would be missed with the edge.
- A customer of one of our resellers had an extremely oversharpened image (huge spatial and frequency domain overshoots), and was unhappy because MTF never dropped to the 20% level, and hence MTF20 could not be measured. In this case we need to educate the reseller that
  - MTF20 is not a good system performance metric, especially for severely oversharpened images. Even MTF50 has its problems, and may not represent system performance, as described in the 2020 paper, [Correcting Misleading Image Quality Measurements](#).
  - Extreme oversharpening degrades system performance, as quantified by object and edge detection metrics SNRi and Edge SNRi, described in [Image Information metrics](#).
  - Because JPEGs from cameras may have severely attenuated Siemens star response at and above  $f_{Nyq}$  (the result of interpolation in low-quality demosaicing; see images 3 and 6), MTF20 and MTF10 can almost always be measured from stars. But this is a spurious result because it is dominated by the lowpass filtering of the demosaicing. It does not represent system performance.

## Conclusions

Both patterns produce similar results below the Nyquist frequency,  $f_{Nyq} = 0.5 C/P$ .

The slanted edge is preferred at **Imatest** because it is more convenient: It is smaller, faster, and better for mapping MTF over the image surface.

Star and edge results can diverge around  $f_{Nyq}$  for images demosaiced in the camera because cameras tend to have lower quality demosaicing than separate raw converters (LibRaw, etc.). This can cause artifacts in edge response and nulls in star response near and above  $f_{Nyq}$ . And they also usually have bilateral filtering.

Raw (sensor) response cannot be reliably recovered from JPEG images captured in cameras. However, much useful information (including a reasonable estimate of information capacity) can still be obtained.

## Miscellaneous notes

### Linear systems and their limits

Imaging systems are mostly [linear](#) (or can be linearized by inverting the [gamma encoding](#) of digital numbers). Linear operations behave in simple, predictable ways: For a linear operation  $H$  on  $x_n(t)$  such that  $y_n(t) = H(x_n(t))$ , then  $\alpha y_1(t) + \beta y_2(t) = H(\alpha x_1(t) + \beta x_2(t))$  [from [Wikipedia](#)]. Standard sharpening and lowpass filtering are linear operations. Unsharp Masking (USM), as commonly defined, is linear, but the MATLAB implementation is not.

Imaging systems, like all linear systems, have limits, and things get interesting when the limits are reached. If imaging systems were perfectly linear, slanted edges and Siemens stars would have identical response. Imaging systems are affected by several types of nonlinearity.

1. **Stray light**, also called [veiling glare or flare light](#), affects measurements when strong light sources (such as the sun) fog the image. In addition to [simple measurements](#), *Imatest* offers [sophisticated hardware for measuring stray light](#).
2. **Saturation**, which occurs then the limits of allowable digital numbers are reached, can cause serious errors in MTF measurements. Saturation can occur when images are under or overexposed, chart contrast is too high, or sharpening is excessive. Described [below](#).
3. **Bilateral filtering**, described in the documentation for [Image information metrics](#)), in which regions of the image close to edges are sharpened (high frequencies are boosted), but regions far from edges are lowpass-filtered (high frequencies are attenuated). Bilateral filtering is nonuniform as well as nonlinear. Almost universal in JPEG files from consumer cameras.
4. **Demosaicing (the primary cause of differences between slanted-edge and Siemens star response)** is a type of interpolation that lowpass filters much of the image, but behaves differently near edges. Discussed [below](#).

## The frequency response of interpolation (which includes demosaicing)

We learned how interpolation affects MTF response when we were struggling with an inconsistency in the image information metrics: Noise Equivalent Quanta (NEQ) was unexpectedly changing when the image was sharpened. The story is chronicled on [Interpolated slanted-edge SFR \(MTF\) calculation](#).

We observed that slanted-edge MTF often had high frequency artifacts that were absent in the Siemens star MTF. We thought these might be the cause of the NEQ inconsistency. To remedy the issue, we applied interpolation to the slanted-edge binning calculation. This made MTF from slanted edged nearly identical to Siemens stars — the high frequency artifacts were eliminated.

But interpolated binning failed to fix the NEQ inconsistency (we eventually found another cause). We realized that interpolation caused the signal to be lowpass-filtered with a  $\text{sinc}^2(fT)$  transfer function for sampling interval  $T$ . This cleaned up the high frequency artifacts in the slanted-edge MTF, but also filtered the Siemens star response, which wasn't obvious because the star had no high frequency artifacts to begin with.

Demosaicing is also a form of interpolation, but with nonuniform processing. It behaves differently in the vicinity of edges, restoring MTF response that would otherwise be filtered out. This accounts for the difference in slanted-edge and Siemens star MTF response, which, as we have observed when preparing this document, is usually much greater for demosaicing in cameras. High quality raw conversion algorithms, such as [LibRaw](#) or [MATLAB Demosaic](#), used in *Imatest*, reduce the discrepancy between MTF results for the two patterns (images 2, 4, 5, and 7).

## Saturation and MTF

When an image saturates (or clips), a sharp corner can form at the boundary of the clipped region that causes the MTF measurement to erroneously increase. Normally saturation happens at the limits of the digital number range defined by the bit depth, for example, 0-255 for bit depth = 8 or 0-65535 for bit depth = 16.

But we sometimes see clipping at other levels, sometimes caused by strange (possibly bad) image processing in prototype cameras, and occasionally in images with specialized color spaces, for example, [Rec. 709](#) only allows digital numbers between 16 and 235 for bit depth = 8. [Rec. 2020](#) also has limits.

It is important to watch for unexpected saturation, which can adversely affect results. Saturation may be less than obvious when only one of the three color channels saturates. Exposure may need to be adjusted to minimize saturation.

## Low quality cameras

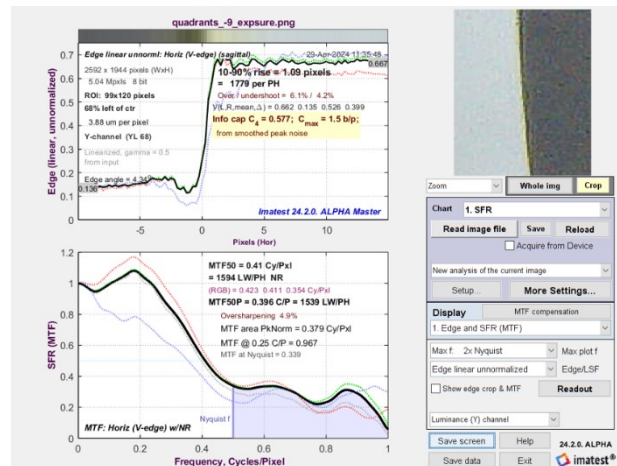
The cameras used in this document were all good quality. I was recently shown images from a cheap camera that appeared to strongly compress the image. (Compression can sometimes be identified by blocking artifacts).

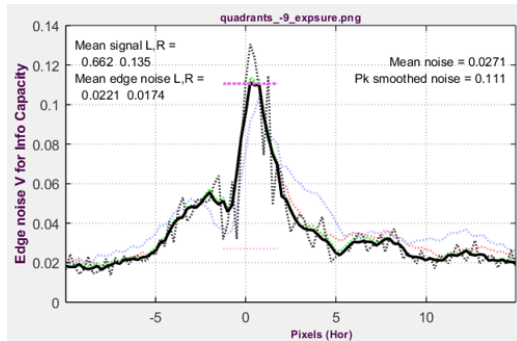
Here is an enlarged portion of a slanted-edge pattern for such a bad image. All sorts of ugly, nasty artifacts are visible.



This image had a high slanted-edge MTF at Nyquist (lower plot on the right), but it had zero sinusoidal response near Nyquist, either due to low-quality demosaicing or bilateral filtering, which appeared to be extremely strong, as indicated by the figure below.

Strong bilateral filtering appears to be the most likely cause of the missing sinusoidal response, but it could also have been caused by the demosaicing. They are difficult to distinguish in “black box” cameras.





In cases like this, neither slanted edge nor Siemens star results by themselves can completely characterize the camera. Both results are required. And charts like [Log Frequency-Contrast](#) add more to the picture.

Simply put the slanted-edge and sinusoidal star response indicate the camera's response to two different types of input.

## Additional references

We compared slanted edges and Siemens stars around 2015, and reached similar conclusions. Here are the links.

[Slanted-edge versus Siemens Star](#) — A comparison of sensitivity to signal processing

[Slanted-edge versus Siemens Star, Part 2](#) — Results for four additional cameras

[Slanted-Edge versus Siemens Star: A comparison of sensitivity to signal processing](#) — a post that has been ignored because it was linked from the [News](#) section of the website.